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高靈敏度主動開口環共振腔  
量測液體介電常數  
High Sensitive Active Split-  
Ring Resonators for Measuring  
Permittivity of Liquid

國立成功大學 電機工程研究所 儀器系統與晶片組  
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(Wireless Innovative Systems EM-applied Lab)

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Wireless Innovation System and  
EM-applied Lab.

# DA-SRR Theory Analysis

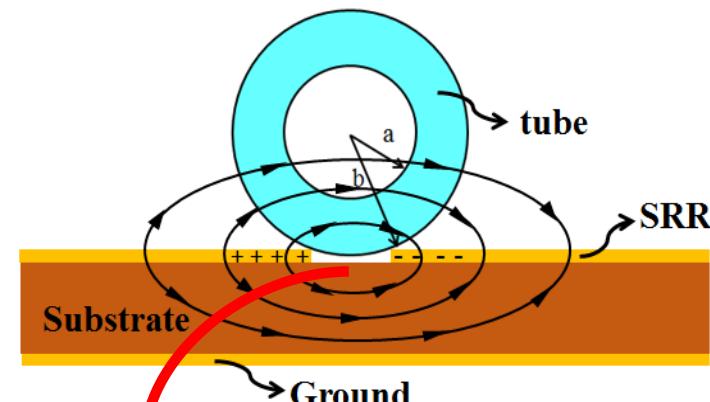
$$\blacktriangleright f_r = \frac{1}{2\pi\sqrt{LC_{total}}} , \quad C_{total} = C_0 + \epsilon_{MUT} C_{MUT}$$

$\blacktriangleright$  High sensitivity theory analysis :

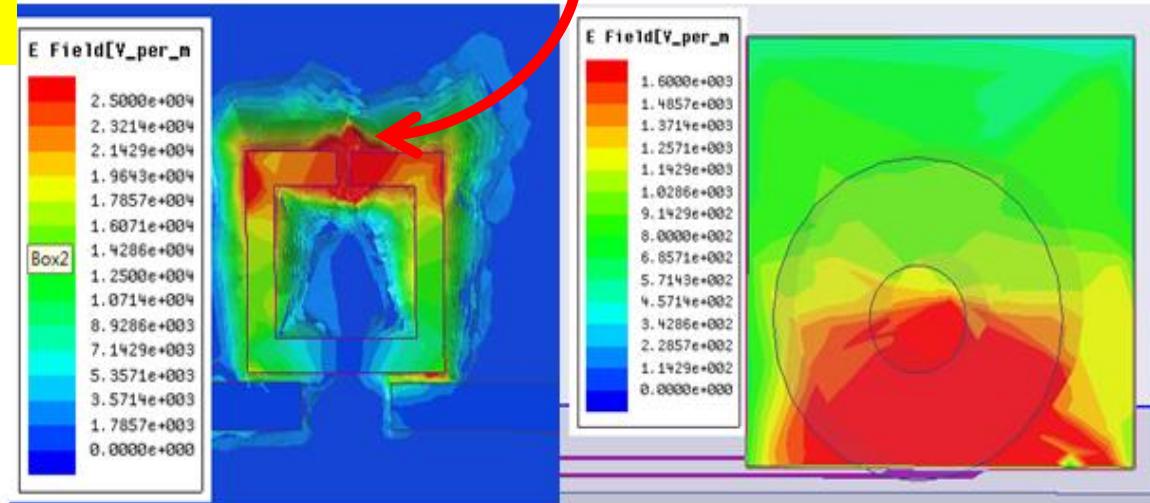
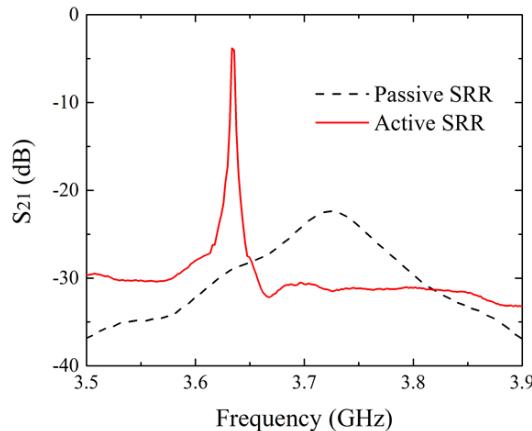
$\blacktriangleright$  High Q property

$$\blacktriangleright U = \frac{1}{2} \epsilon_0 \int E^2 dV = \frac{1}{2} \epsilon_0 E_0^2 V_m \quad , \quad V_m \cong \int \frac{E^2}{E_0^2} dV$$

$\blacktriangleright V_m$  is the volume of the penetration of the  $E$  field

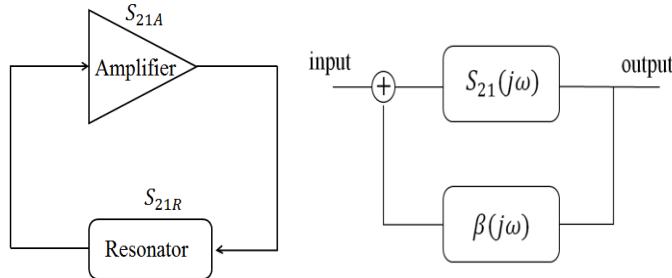


The Q factor is enhanced by 22 times

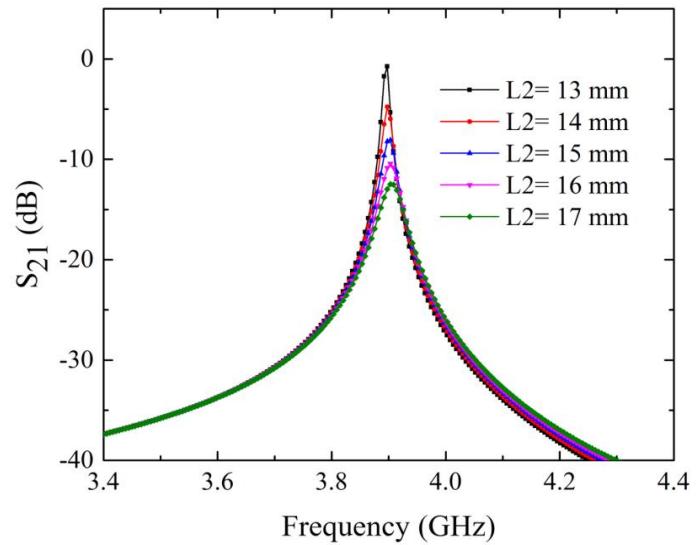
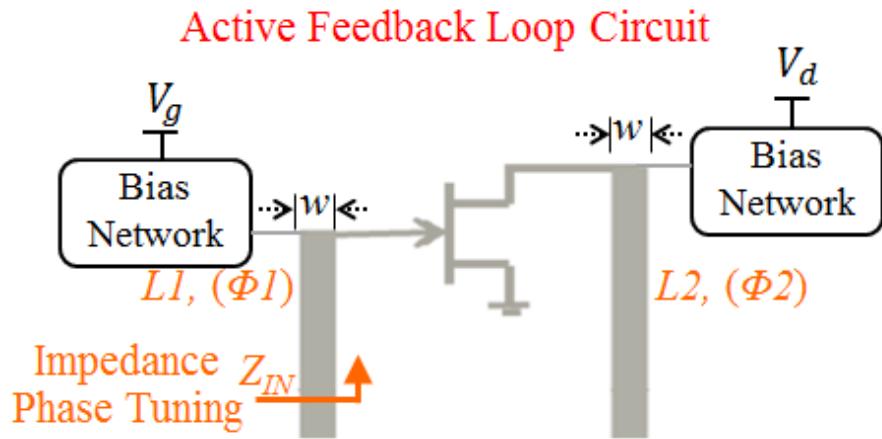


# DA-SRR Design

- Active feedback loop method
- $H(j\omega) = \frac{S_{21}(j\omega)}{1 - S_{21}(j\omega) * \beta(j\omega)}$
- Simulation optimal Q = 1265

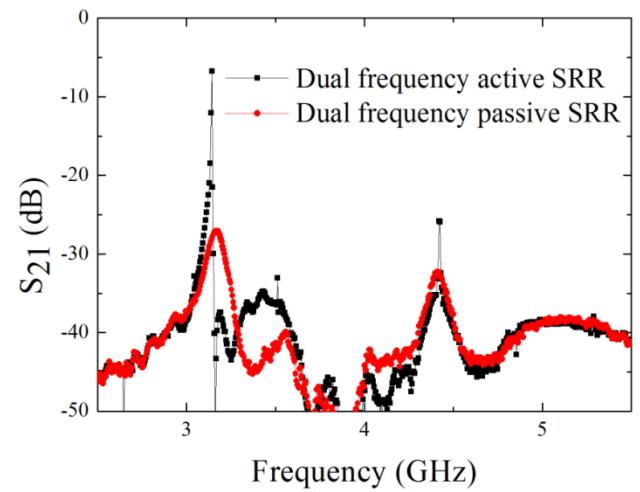
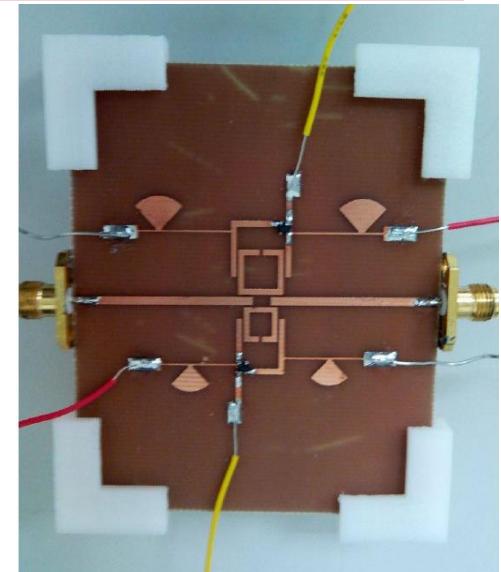
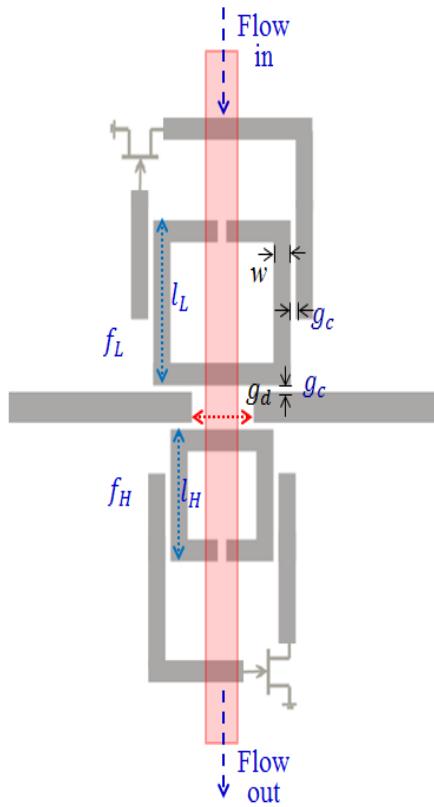
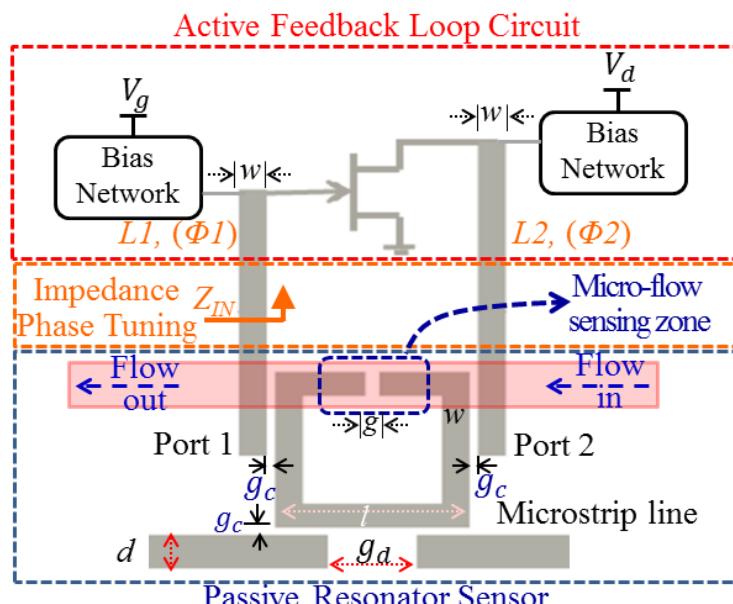


- DA-SRR calibration technique
- $\epsilon_{eff} \propto f_r^{-2}$
- $\epsilon_{eff} = 1 + (\epsilon_{rMUT}' - 1)q_1 + (\epsilon_{tube}' - 1)q_2$
- $f_{rL}^{-2} = S_1(\epsilon_{rMUT}' - 1) + f_{L0}^{-2} + E_{tube} * f_{L0}^{-2}$
- $f_{rH}^{-2} = S_2(\epsilon_{rMUT}' - 1) + f_{H0}^{-2} + E_{tube} * f_{H0}^{-2}$



# DA-SRR Structure

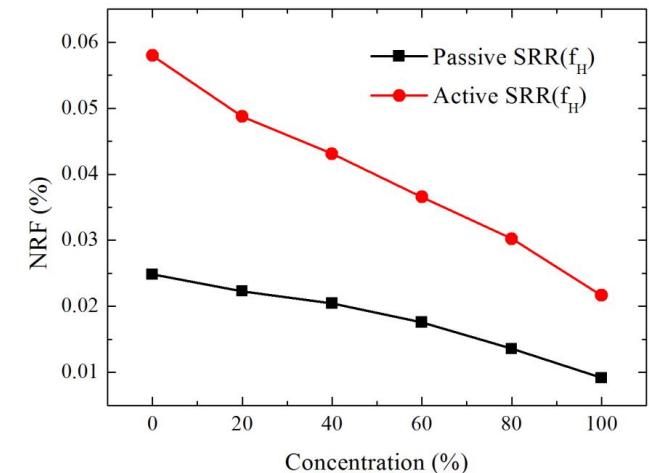
- DA-SRR circuit structure
- $l_L = 8 \text{ mm}$ ,  $g = 0.5 \text{ mm}$ ,  $w = 1 \text{ mm}$ ,  $g_d = 3.5 \text{ mm}$ ,  
 $l_H = 6 \text{ mm}$  and  $g_c = 0.3 \text{ mm}$   $\circ f_{L0} = 3.1291 \text{ GHz}$ ,  
 $f_{H0} = 4.4745 \text{ GHz}$   $\circ$
- $Q_L = 1023$  ,  $Q_H = 984$



# Experiment Results

- The Q factor of sensor is enhanced by 22 times from (passive SRR) 49.7 to 1098.
  - The sensitivity is improved by 2.3 to 3.7.
  - Average error : 4.5 %
- Passive SRR Sensor:

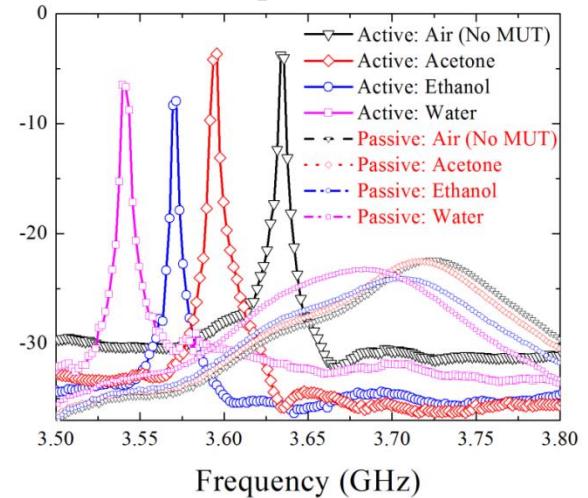
Parameter	$f$ (GHz)	$Q$	$S_{21}$ (dB)	$\Delta f/f_{air}$ (%)	$(\Delta f/f_{air})/\Delta \varepsilon_r$ (%)
Air (no MUT)	3.7257	49.7	-22.4	---	---
Acetone	3.7157	35.7	-22.5	0.27	0.013
Ethanol	3.7078	49.0	-24.1	0.48	0.02
Water	3.6834	36.4	-23.3	1.10	0.014



DA-SRR and Dual passive SRR sensors

Active SRR Sensors:

Parameter	$f$ (GHz)	$Q$	$S_{21}$ (dB)	$\Delta f/f_{air}$ (%)	$(\Delta f/f_{air})/\Delta \varepsilon_r$ (%)
Air (no MUT)	3.6336	1098.4	-3.81	---	---
Acetone	3.5955	1016.4	-3.67	1.00	0.048
Ethanol	3.5836	1041.2	-4.89	1.37	0.057
Water	3.5412	728.0	-6.50	2.54	0.031



The measured  $S_{21}$  performance of various solvents

